



**BC Performance Standards** 

# Numeracy



**BC Performance Standards** 



**REVISED EDITION** 



#### ACKNOWLEDGMENTS

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# About the BC Performance Standards

he BC performance standards have been developed for voluntary use in BC schools. They describe the professional judgments of a significant number of BC educators about standards and expectations for the following key areas of learning:

- reading
- writing
- numeracy
- social responsibility

The standards focus exclusively on *performance assessment*. In performance assessment students are asked to apply the skills and concepts they have learned to complete complex, realistic tasks. This type of assessment supports a criterion-referenced approach to evaluation and enables teachers, students, and parents to compare student performance to provincial standards.

The BC performance standards are intended as a resource to support ongoing instruction and assessment. Teachers can use these standards to:

- monitor, evaluate, and report on individual student performance
- identify students who may benefit from intervention
- develop a profile of a class or group of students to support instructional decision-making
- prompt discussions with parents, students, and other teachers about student performance
- inform professional development activities
- collaboratively set goals for individuals, classes, or schools
- develop evidence for school growth plans
- provide models for designing performance tasks

## Performance standards support ongoing instruction and assessment.

## **Ongoing Development**

#### **REFERENCE SET CONNECTION**

The BC performance standards are a continuation of the work begun in the provincial reference sets.

Starting in 1991, the province developed reference sets for reading, writing, mathematical development, group communication skills, and problem solving. The reference sets show the broad range of possible student development in each of these essential skill areas. They can be used to evaluate student work in any subject.

The BC performance standards work within these same ranges of development in the same areas. They can also be used to evaluate these skills in any subject. However, the standards focus on levels of performance at particular grades.

For both sets of documents, teachers used their experience and student work to develop and validate the materials. Both also use student work and teacher comments to illustrate and describe levels of performance.



#### LEARNING OUTCOMES

Learning outcomes describe what students are supposed to learn in each subject and at each grade level. Learning outcomes are often called *content standards*. Content standards answer the question: "What knowledge, skills, and attitudes are students expected to develop at this grade level?"

The ministry's Integrated Resource Packages list prescribed learning outcomes for BC provincial curricula for each subject and grade level.

The BC performance standards complement existing curricula and assessment materials developed by the Ministry of Education.

## **Ongoing Development**

#### PERFORMANCE STANDARDS

Performance standards describe levels of achievement in key areas of learning. Performance standards answer the questions: "How good is *good enough?* What does it look like when a student's work has met the expectations at this grade level?"

The BC performance standards describe and illustrate the following four levels of student performance in terms of prescribed learning outcomes relevant to the key areas of reading, writing, numeracy, and social responsibility.

#### NOT YET WITHIN EXPECTATIONS

- the work does not meet grade-level expectations
- there is little evidence of progress toward the relevant prescribed learning outcomes
- the situation needs intervention

## **MEETS EXPECTATIONS (MINIMAL LEVEL)**

- the work may be inconsistent, but meets grade-level expectations at a minimal level
- there is evidence of progress toward relevant prescribed learning outcomes
- the student needs support in some areas

## FULLY MEETS EXPECTATIONS

- the work meets grade-level expectations
- there is evidence that relevant prescribed learning outcomes have been accomplished

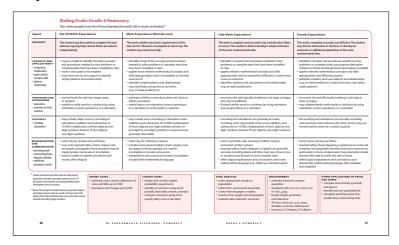
## EXCEEDS EXPECTATIONS

- the work exceeds grade-level expectations in significant ways
- the student may benefit from extra challenges

The standards describe and illustrate four levels of performance.

## **Key Components**

These key components are included for each grade level. **Rating Scale.** This is the full version of the performance standards, with the four performance levels described in detail.



Aspect	Not Yet Within Expectations	Meets Expectations (Minimal Level)	Fully Meets Expectations	Exceeds Expectations	
INAPINOT	The student may be unable to complete the task without ongoing help; cannot fallow procedures independently.	The work satisfies most basic requirements of the task, but it is flawed or incomplete in some way. The student may need some help.	The work is complete and accurate (may include minor errors). The student is able to develop a simple extension.	The work is complete accurate, and efficier The student may find an alternative or a shortcut, or develop o extension.	
CONCEPTS AND APPLICATIONS* • secapizing mathematics • grade-specific concepts,skills • pallens, solutionships	may be unable to identify basic concepts and procedures needed work is inaccurate or incomplete may need costo-core support to identify simple patterns and relationships	identifies some concepts and procedures needed     apples most relevant concepts and skills appropriately, some erron or consistons identifies simple patterns and relation- ships if prompted (e.g., to make predictions)	<ul> <li>Identifies concepts and procedures needed</li> <li>applies relevant</li> <li>concepts and skille; may be acrowshat inefficient or make minor errors</li> <li>Identifies, suplains, and uses simple patterns and relationships</li> </ul>	<ul> <li>Identifies concepts and procedures needed may proper alternative solution applies relevant concepts and skills efficiently, precise identifies, explains, and uses patterns a relationship; may notice subtle patte</li> </ul>	
STRATEGIES AND APPROACHES • procedures • estimates to serify solutions	cannot break the task into stages, steps, or sections     unable to verify results or solutions	tries to follow     instructions; does not     check or adjust     procedures     needs help to verify     results or solutions	<ul> <li>structures the task logically; may be inefficient</li> <li>if asked, verifies results or solutions</li> </ul>	<ul> <li>structures the task efficiently</li> <li>may independently verify results or solutions</li> </ul>	
ACCURACY • recording, calculations	<ul> <li>may include major errors in recording or calculations</li> </ul>	<ul> <li>may include some recording or calculation error; comparisons are generally reasonable</li> </ul>	<ul> <li>recording and calculations are generally accurate; may be minor errors</li> </ul>	<ul> <li>accurate recording and calculations, including unit;ma use mental math</li> </ul>	
REPRESENTATION AND COMMUNICATION • presenting work • constructing dwirt, diagram, display • explaining procedures, results	work may be unclear and contuing may omit or make major errors in tables, charts, displays, disparse may be unable to explain procedures and results	<ul> <li>work may be confusing in places</li> <li>includes most required tables, charts, displays, and diagrams; come errors or ornisalons</li> <li>explanations and conclusions may be incomplete; little mathematical language</li> </ul>	work is generally clear, easy to follow required tables, charts, graphs, and diagrams are generally accurate; minor errors or omissions offers logical explanations and conclusions, some mathematical language	work is clear and ea to follow     required tables, cha graphs, diagrams as accurate and compl offers logical explanations and conclusions; uses mathematical language	

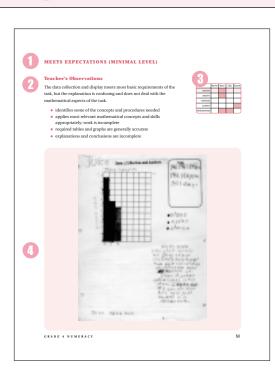
**Quick Scale.** This is a short-form summary of the *Rating Scale. Quick Scales* are intended for daily use. Teachers may also want to share them with students and parents.

Sample Tasks. These are tasks developed by practising teachers to provide opportunities to assess student work in the skill area. Each sample task includes examples of student work. Teachers may use the tasks as given or as models. Any tasks used should first be reviewed for issues sensitive to the class or community.

con	TEXT
	was the culminating activity in a data collection unit. During the
	the teacher modelled and provided several opportunities for
	ents to practise matching questions to a sample population,
colle	cting data, and constructing and analyzing graphs.
мат	REMATICAL CONCEPTS
	select appropriate sample or population
	collect first- and second-hand data
	create interval graphs/tables
	construct bar graphs
	evaluate data collection processes
PRO	CESS
The	class reviewed what they had learned about conducting surveys
and	communicating the results. The teacher explained that for this
sure	ey, each student would choose his or her own question and work
inde	pendently to collect and display the data. The class brainstormed
som	e possible questions.
Stud	ents then worked independently to:
	Choose a survey topic.
2	. Survey the sample population (usually their classmates) and tally the results.
3	. Create a bar graph to display the data collected.
4	<ul> <li>Analyze the data: write a short summary of the results (e.g., range, most frequent choice, number of people).</li> </ul>
5	Evaluate the survey (e.g., comment on the sample and the data collection).
6	Post the work around the room for other students to view.
	class discussed what they had learned and commented on ways that
	projects were similar and different. They also developed a list of
	" for collecting and displaying data, which the teacher posted for
	reference. For the remainder of the school year, the teacher
	suraged students to look for situations where they could collect and
repo	rt on data in other subject areas.

Additional sample tasks, student work, and other support materials are available at the Ministry of Education's web site.

## **Student Samples**



For each task there is one example of student work at each of the four levels.

## Level of Work.

- **Teacher's Observations.** These are additional comments by the teacher and key relevant criteria from the *Rating Scale*.
- 3 **Rating Scale Icon.** This is a generalized summary of the scale completed by the teacher. Here is how the actual scale looks for this sample:

_		ny time of the year, depending who			_				
Aspect	Not Yet Within Expect	ations	Meets Exp	ectations (Minimal Level)		Fully Meets Expectations		Exceeds Expecta	tions
SNAPSHOT	The student may be unable to complete the task without ongoing help; cannot follow procedures independently.		The work satisfies most basic requirements of the task, but it is flowed or incomplete in some way. The student may need some help.		The work is complete and accurate (may include minor flaws or erron). The student is able to develop a simple extension of the same mathematical idea.		The work is complete, occurote, and efficient. The student may find an alternative or shortcat, or develop an extension or additional application of the same mathematical idea.		
CONCEPTS AND APPLICATIONS** • Neophing mathematics • grade-specific encopts, skills • pathens, Nilationships	• may be unable to identify the basic concepts     and procedures needed to solve problems or     complete such that has been been modified in clean     work is inaccanate or incomplete     may need on-to-one support to dentify     simple patterns and relationships		I - Another sums of the convertient and procedures exected to a low plane run competent water the here been modelified in class applies most indeximited concepts and ability appropriately vanish is incomplete or includes - another appropriately vanish is incomplete or includes - another appropriately vanish is incomplete or includes - another appropriately vanish is not used them (e.g., to make prediction)		identifies concepts and procedures needed to solve problems or complete tasks the have been modelled in class     applen relevant mathematical accesspts and skills appropriatively pays to smershale tables of the minor errors or omissions     identifies, explaint, and uses patterns and relationships (e.g. to make predictions)		identifies concepts and percedures needed to solve problems or complex tasks, may propose alternative solutions on vhortunit hug beyong percedures modeled a spplin relevant mathematical concepts and skills appropriately and efficiently, previous left, for make predictions, reade shortcosts), may notice subtle patterna.		
STRATEGIES AND APPROACHES • procedures • extendes to verify solutions	<ul> <li>cannot break the task into stages, steps, or sections</li> <li>unable to verify results or solutions by using estimation, inverse operations, or a calculator</li> </ul>		<ul> <li>attempts to follow instructions; does not check or adjust procedures</li> <li>needs help to use estimation; inverse operations; or a calculator to verify results or solutions</li> </ul>		structures the task logically, breaking it into steps or stages, but may be inefficient     if asked, verifies results or solutions by using estimation, inverse operations, or a calculator		structures the task efficiently, breaking it into logical steps or stages     may independently verify results or solutions by using estimation, inverse operations, or a calculator		
ACCURACY • scording calculations	<ul> <li>may include major errors in recording or calculations (addition and subtraction to 10 000; multiplication of three-digit by one- digit numbers; division of two-digit by one-digit numbers)</li> </ul>		<ul> <li>may include some recording or calculation errors (addition and subtraction to 10 000; multiplication of these-diplic by one-digits unberec, division of two-digits by one-digit numbers); comparisons are generally reasonable</li> </ul>		<ul> <li>recording and calculations are generally accurate, including units; may include minar enersy (addition and subtraction to 10 000; multiplication of three-digit by one- digit numbers; division of two-digit by one-digit numbers)</li> </ul>		<ul> <li>all recording and calculations are accurate, including units (exercise some tolerance for minor enrors); may use mental math to arrive at a solution quickly</li> </ul>		
REPRESENTATION AND COMMUNICATION - presenting work - constructing charts, diagrams, displays - explaining proordures, results	c ATION may ornit required tables, charts, super, nets, bar graphs, pictograph; those provided may be imppropriate, maccurate, or incomplete may be unable to explain procedures and results; often illogical		each may be conclusing to places     each may be conclusing to places     preclases more regiment blacks, charter, but may be     incomplete to inclusion plank, but may be     incomplete to inclusions may be     incomplete to inclusions may be     incomplete to incomplete;     includes limite mathematical language		vorkin sprenzely dear and say to follow may be sensewhat much by in glasses:     request stables, durit, diagram, ce graphia are greenely accurate including liabels and there may have minor and accurate including liabels and there may have minor and offen liagrad explanations and conclusion; uses some mathematical language (e.g., added ig, nitrosted, equal)		<ul> <li>work is clear and easy to follow         <ul> <li>required tables, charts, dagrams, or graphs are accounte and complexity, fold-tables, that is lensy have mirror errors, particularly in more complex taskit, may volk tably include features that help to clerify the task or result</li> <li>offen logical explemations and conclusion; saws appropriste mathematical language, often detailed and imightful</li> </ul> </li> </ul>		
Development Across Carries "Some of the concepts and sk consoleting numerors tiples	endly enables the lev <sup>2</sup> 2/3 set 'bulkating Mathematical dam. Hustademh are expected to apply in are specific to the type of task. The tion 'bulk to the type of task. The tion bulk of the second	MONEY TASKS • etimate,count, record co coins and bills up to \$100 • purchases and change up		CHANCE TASKS • design and conduct simple probability experiments • identify an outcome suing terms possible, impossible, centain, uncertain • compare outcomes using terms equally, <i>likely</i> , more or less likely		DATA ANALYSIS • select appropriate sample or population • collect finite- and second-hand data • create interval graphs or tables • contract bare graphs and pictoraphs • evaluate data collection processes	HEASUREMENT • estimate, measure quantities • standard units:mr m <sup>2</sup> /ml,1, g, kg • length, height, per circumference • 24-hour clock; am decades, centuries • construct: 2-D shas	, cm, m, km, cm <sup>2</sup> , meter, ,p.m.; yean, ,millenniums	OTHER APPLICATIONS OF SPACE AND SHAPE - compare and contrast pyramids and prims - identify and sort quadrilatensis - identify and dort point, line, panallel line, intersecting lines

**Student Work.** This shows a reproduction of the student's work. (Names of students and teachers have been changed where this information could be used to identify individuals.)

ABOUT THE BC PERFORMANCE STANDARDS

## **Using the Standards**

The BC performance standards can contribute to a comprehensive assessment and evaluation svstem. eachers use a variety of methods to gather the information they need to assess, evaluate, and report on student learning. Possible methods include classroom and standardized tests, observations, student work portfolios, conferences, self- and peer assessment, and performance tasks.

The BC performance standards give teachers a way to assess students' abilities to apply their learning in realistic performance tasks in the areas of reading, writing, numeracy and social responsibility. Used with other methods, they can be an important part of a comprehensive assessment and evaluation system. The standards:

- should be used within the context of ongoing classroom instruction. They are meant to be curriculum-embedded—used as part of regular classroom learning activities.
- provide resources for assessing and evaluating the quality of a specific piece or a collection of student work from various subject areas. They can help to develop a profile of student achievement, typically based on three to seven pieces of work.
- assume that in most cases teachers are observing students as they work. Often, some of the evidence needed to make decisions about a student's work comes from observations and conversations with students.
- allow for teachers to intervene where students are unable to complete a task independently. The level of assistance required is often one of the criteria for determining whether or not a student's work falls within grade-level expectations.
- may be adapted as needed. This might mean creating scales for grades not included in the standards, developing IEPs or other tailored evaluation, or adjusting expectations for different times of the year.

## **Supporting Learning**

he BC performance standards are intended to support instructional decision-making. Teachers may want to consider the following questions as they plan instruction:

- How do these standards match my/our expectations for students at this level?
- What kinds of instructional strategies and learning opportunities will help most students develop the skills they need to meet these expectations?
- What additional support and interventions will be needed to help *all* students meet these expectations?
- If there are some students for whom these expectations are *not* appropriate, what expectations should they meet?
- What evidence do I/we need to collect to find out if students are making progress towards the expectations?

The BC performance standards can be used to help plan instruction.

# **Numeracy in BC Schools**

*umeracy* refers to the application of mathematical understanding in daily activities at school, at home, at work, and in the community. It involves both using mathematical skills and knowing how mathematics can be used to solve problems.

Just as there is more to literacy than teaching the rules and procedures of language, there is more to numeracy than teaching the rules and procedures of mathematics. Numerate individuals not only "know" mathematics, but understand it in personally meaningful terms. They feel competent and confident about their ability to draw on the necessary knowledge and apply it in new and relevant ways.

## **Numeracy and Mathematics**

W umeracy as a skill area is currently evolving in the BC school system. The following is the understanding of the term as it is used in this document. This may be refined and adjusted as our understanding improves.

Numeracy involves concrete applications in which students, confidently and independently, use mathematics to address real tasks or problems in an increasing variety of situations. The ability to recognize the mathematical demands and possibilities in a situation is an important aspect of numeracy.

Numeracy is based on mathematical foundations and requires the application of concepts and skills related to the formal aspects of the discipline of mathematics. These formal aspects are reflected in the organizers for BC mathematics curricula:

- Number (Concepts and Operations)
- Patterns and Relations
- Shape and Space
- Statistics and Probability
- Problem Solving (Grades 8-12)

Numeracy tasks and problems typically draw on concepts and skills from two or more of the curriculum organizers listed above, and can be grouped according to purpose or context. For example, Human Resources Development Canada describes numeracy as an *essential skill* and identifies five contexts or applications in which adults are required to apply mathematical concepts and skills in the workplace:

- money math
- scheduling or budgeting and accounting math
- measurement and calculation math
- data analysis math (including chance)
- numerical estimation

## **Part of a Comprehensive Picture**

The BC performance standards for numeracy can be used to evaluate students' abilities to use the mathematics they have learned to address concrete, practical, and age-appropriate tasks and problems. The performance standards do *not* address all aspects of the mathematics curricula and need to be used in combination with other forms of assessment to develop a comprehensive picture of student achievement in the BC mathematics curricula.

Although this document currently includes only grades 1 through 8, it is the intention that numeracy be a focus in BC classrooms from Kindergarten to Senior Secondary. Work is ongoing in this area.

## **Curriculum Connection**

In BC schools, primary responsibility for developing and evaluating mathematical skills is assigned to mathematics. Depending on the tasks developed or selected, using the numeracy standards can help teachers address a wide range of outcomes from the provincial mathematics curricula.

However, students are expected to apply and extend their numeracy skills in a variety of content areas (e.g., map reading/making in social studies; constructing/interpreting data tables and graphs in science; data analysis and evaluation in areas such as history, English language arts, and career and personal planning; tracking progress in physical education; using perspective in visual arts). The performance standards for numeracy have therefore also been developed to apply in all curriculum areas.

## **Aspects of Numeracy**

The performance standards focus on four aspects of numeracy, as described here.

#### **CONCEPTS AND APPLICATIONS**

- recognizing the mathematical demands and possibilities in a situation or task
- applying grade-specific concepts and skills
- recognizing and using patterns and relationships

Evidence comes from observing and talking to students and analyzing their work. In school, many numeracy tasks simulate real applications (rather than having students find problems to solve on their own) and thus do not provide evidence of ability to recognize the mathematical possibilities in a situation.

## STRATEGIES AND APPROACHES

- structuring the task into logical steps or stages
- verifying solutions

Evidence comes from observing and talking to students and analyzing their work. With younger students, most evidence comes from observation. Older students may clearly demonstrate these features in their written work if the task is structured to require it.

## ACCURACY

recording and calculations

Evidence comes from examining student work.

## **REPRESENTATION AND COMMUNICATION**

- presenting work
- constructing charts, tables, diagrams, and displays
- explaining procedures and results

Evidence of presentation and construction comes from examining student work. It is usually necessary to prompt students to specifically explain procedures and results. Evidence of this aspect is most effectively gathered through conferences; however, students can also provide written explanations.